

HALL TICKET NUMBER

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PACE INSTITUTE OF TECHNOLOGY & SCIENCES::ONGOLE
(AUTONOMOUS)

II B.TECH I SEMESTER END SUPPLEMENTARY EXAMINATIONS, MARCH/APRIL - 2023
Mathematical Foundation of Computer Science
(Common to IT, AIML Branches)

Time: 3 hours

Max. Marks: 60

Note: Question Paper consists of Two parts (Part-A and Part-B)

PART-A

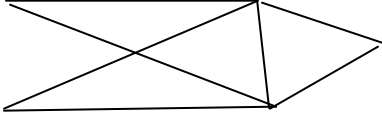
Answer all the questions in Part-A (5X2=10M)

Q.No.	Questions	Marks	CO	KL
1	a) List all implications in statement calculus.	[2M]	1	
	b) Define compatibility relation?	[2M]	2	
	c) Compute 8_{p_5} and 6_{p_3} .	[2M]	3	
	d) Write about partial fraction decomposition.	[2M]	4	
	e) What are bipartite graphs?	[2M]	5	

PART-B

Answer One Question from each UNIT (5X10=50M)

Q.No.	Questions	Marks	CO	KL
UNIT-I				
2.	a) Assume x is a particular real number. Determine whether the following two statements are logically equivalent. (i) $x < 2$ or it is not the case that $1 < x < 3$ (ii) $x \leq 1$ or either $x < 2$ or $x \geq 3$.	[5M]	1	
	b) Prove that the following argument is valid: No engineers are fools. No one who is not a fool is an administrator. Kumar is an engineer. Therefore Kumar is not an administrator.	[5M]	1	
OR				
3.	a) Find the truth table for the propositional formula: $(p \leftrightarrow q) \leftrightarrow (q \rightarrow p)$.	[5M]	1	
	b) Explain pcnf and find pcnf of the formula $(\neg P \rightarrow R) \wedge (Q \leftrightarrow P)$.	[5M]	1	
UNIT-II				
4.	a) Let $f = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 2 & 4 & 1 & 3 \end{pmatrix}$ and $g = \begin{pmatrix} 1 & 2 & 3 & 4 \\ 4 & 1 & 2 & 3 \end{pmatrix}$ find $(f \circ g)$ and $(g \circ f)$.	[5M]	2	
	b) Let $X = \{1, 2, 3, 4\}$ be a set and R is a relation on the set X such that $R = \{(1, 1), (1, 4), (4, 1), (4, 4), (2, 2), (2, 3), (3, 2), (3, 3)\}$. Draw its matrix and graph. Also prove that R is an equivalence relation.	[5M]	2	
OR				
5.	a) Let $A = \{1, 2, 3, 4\}$ and f and g be functions from A to A given by $f = \{(1, 4), (2, 1), (3, 2), (4, 3)\}$ and $g = \{(1, 2), (2, 3), (3, 4), (4, 1)\}$ prove that f and g are inverse of each other.	[5M]	2	
	b) Explain in brief about Inversive and Recursive functions with examples.	[5M]	2	
UNIT-III				
6.	a) Find the coefficient of $x^9 y^3$ in the expansion of $(2x - 3y)^{12}$.	[5M]	3	
	b) In any group $(G, *)$, by proving the inverse of every element is unique.	[5M]	3	
OR				

7.	a)	Find the number of permutations of the EVERGREEN word?	[5M]	3	
	b)	Let $G = \{-1, 0, 1\}$. Verify that G forms an abelian group under addition?	[5M]	3	
UNIT-IV					
8.		Suppose a continuous random variable x has the probability density function is $f(x) = k(1-x^2)$ for $0 < x < 1$ then find (i) k (ii) Mean and (iii) variance	[10M]	4	
OR					
9.	a)	Solve the recurrence relation $a_n - 6a_{n-1} + 9a_{n-2} = 0$ for $n \geq 2$ given $a_0 = 5, a_1 = 12$.	[5M]	4	
	b)	Solve the recurrence relation $a_{n+2} - 4a_n = 9n^2$.	[5M]	4	
UNIT-V					
10.	a)	Define Eulerian circuit and Hamiltonian circuit, give an example of graph that has neither Eulerian circuit nor Hamiltonian circuit.	[5M]	5	
	b)	Explain isomorphism of two graphs with suitable example.	[5M]	5	
OR					
11.	a)	Explain Kruskal's algorithm to find minimal spanning tree of the graph with suitable example. Find minimal spanning tree for the given graph.	[5M]	5	
					
	b)	Explain about DFS and write the algorithm of DFS with example.	[5M]	5	
